In Pursuit of 
Quality Mathematics Education for All 
Proceedings of the 
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In Pursuit of Quality Mathematics Education for All
Proceedings of the 7th ICMI-East Asia Regional Conference on Mathematics Education

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Introduction

The mark of an excellent academic conference is the high quality of papers delivered and published in its proceedings. It is the pride of every International Program Committee of a conference to have an outstanding collection of papers that enlighten, inspire and most of all, contribute new knowledge to the field.

This book contains original, unpublished papers, especially written and prepared for EARCOME 7. Some papers are derivatives of previous works that have not been shared in EARCOME while others are continuation of works presented in past EARCOMEs.

I thank all our colleagues and friends who chose to present their work and send their papers for the proceedings to materialize. I commend the invited speakers for their enthusiasm in sharing their ideas, even if it meant they took the extra time to write when they could have easily declined the request to do so. I am also grateful to the TSG presenters who eagerly sent their full papers for review. Blind reviews are never an easy process; however, it is a necessary part of our academic life and it makes us all better scholars.

In finalizing this book, I needed the extra help from two individuals whom I could quickly call on. I thank Dr. Mary Thomas for her patience and expertise in the English language. I also thank Rebecca Yu for assisting me every night when I needed her skills.

I hope you take the chance to read each and every paper. I assure you that they are all worth your time.

The Editor
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